Everything you want to know about bridge courses-except whether they work. *Preliminary findings from a national survey* (Slides for a talk given at the Joint Mathematics Meetings 2007, New Orleans)

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Idea for the survey

From catalogs, gather basic data about bridge courses, including

- How many US colleges/universities list a bridge course in their catalogs?
- How many US colleges/universities require a bridge course for the mathematics major?
- What are the most common topics listed in the catalog descriptions of bridge courses?

Real question: Do bridge courses work?

"Working" definition

- Students leave a bridge course recognizing the role and nature of proof in mathematics;
- students can write basic proofs properly;
- students write better proofs in their subsequent coursework; and
- students do all of that better than they would have "the old way," before bridge courses.

Straw poll

List the 2 - 3 topics that you think are essential for a bridge course.

Topic		

Your overall confidence level 1-10 (10 = high confidence) that proofs courses "work."

Bridge Course Definition for the survey

Explicitly described as a bridge course **or** *two* of the following criteria are met:

- Catalog course description prominently mentions mathematical proofs.
- Catalog course description implies transition or bridge to advanced undergraduate courses.
- Catalog course title includes "proof" or the title is one commonly associated with bridge courses: "Transition to Higher Mathematics", "Foundations of Mathematics", "Fun-damentals of Mathematics", . . .

And the title and primary course content is not discrete mathematics, linear algebra, real analysis, abstract algebra, geometry, or formal/symbolic logic.

Personal History of Bridge Courses

Pre-1983 Students expected to learn proofwriting by observation

May 1983 - Bucknell instituted Writing Across the Curriculum

Summer 1984 - Three courses became the department's "Writing within the Discipline" courses through the inclusion of explicit instruction in proof writing

Summer 1994 - Designed a bridge course for Bucknell to replace most of the proof writing instruction in the above three courses

Winter 1998 - Designed a bridge course for Western Oregon University.

Survey Methodology

From the 1,431 institutions on the AMS lists used for "Annual Survey of the Mathematical Sciences," we randomly chose 20% from each category (Groups I, II, III, M, and B). (Discarded institutions without bachelors degrees in math.)

Searched catalogs for the desired information.

Recorded the information in a data base.

Results: Frequency

Bridge course in catalog	39.6%
Bridge course required for major	32.6%
No bridge, but discrete w/ proofs	22.0%
Discrete w/ proofs required	16.3%
No bridge, no discrete, but some other w/ proofs Some other w/ proofs required	15.9% 9.8%

Results: Topics

Set Theory	83.5%
Logic	78.3%
Functions	55.7%
Relations	54.6%
Methods of proof	40.2%
Induction	33.0%
Equivalence relations	18.6%
Number theory	15.5%
Real numbers	9.2%

Assessment: Do bridge courses work?

E-mail sent to institutions having bridge courses:

"In preparation for a panel discussion at the 2007 Joint Mathematics Meetings, we are gathering some data about courses like your [bridge course], which seems to include instruction in proof writing. We want to ask just two yes/no questions. ...

1. Has anyone done assessment of [your bridge course] to determine its effectiveness in helping students write better proofs in their subsequent coursework?

2. If "yes", would you be willing to share the results of the assessment with us? ..."

Results: Assessment

60% (58 of 97) responded.

Answered "yes" to Question 1	2
Assessment planned for this year	3
Volunteered a positive opinion	15
Confessed uncertainty	1
(Assessed in-course improvement	2)