

ES476/576 Hydrology

Review Problems: Physical Properties of Water

Show all of your math work and unit algebra below. Draw a sketch where required.

1. Determine the following pressure equivalents:

- a. Average atmospheric pressure at the Earth's surface is 1013 millibars (mb) (weight of a column of air pressing down on you; determine the pressure equivalent in:

$$\begin{aligned} \text{psi} &= 14.69 & 1.013 \text{ bar} \cdot \frac{14.5 \text{ psi}}{\text{bar}} \\ \text{bar} &= 1.013 & 1013 \text{ mb} \cdot \frac{\text{bar}}{1000 \text{ mb}} \\ \text{Pa} &= 101300 & 1.013 \text{ bar} \cdot \frac{100 \text{ kPa}}{\text{bar}} \cdot \frac{1000 \text{ Pa}}{\text{kPa}} \\ \text{kPa} &= 101.3 \end{aligned}$$

- b. At the deepest depths of the ocean along the Mariana trench, hydrostatic pressure is approximately 1086 bars; determine the pressure equivalent in

$$\begin{aligned} \text{psi} &= 15747 & 1086 \text{ bar} \cdot \frac{14.5 \text{ psi}}{\text{bar}} \\ \text{mb} &= 1.086 \times 10^6 & 1086 \text{ bar} \cdot \frac{1000 \text{ mb}}{\text{bar}} \\ \text{Pa} &= 1.086 \times 10^8 & 1086 \text{ bar} \cdot \frac{100 \text{ kPa}}{\text{bar}} \cdot \frac{1000 \text{ Pa}}{\text{kPa}} \\ \text{kPa} &= 108600 \end{aligned}$$

- c. The base of the Earth's continental crust is at a depth of approximately 10 km, with a lithostatic pressure equivalent of 10 Kb (kilobars); determine the pressure equivalent in

$$\begin{aligned} \text{psi} &= 145000 & 10 \text{ Kb} \cdot \frac{1000 \text{ bar}}{\text{Kb}} \cdot \frac{14.5 \text{ psi}}{\text{bar}} \\ \text{mb} &= 1.0 \times 10^7 & 10000 \text{ bar} \cdot \frac{1000 \text{ mb}}{\text{bar}} \\ \text{Pa} &= 1.0 \times 10^9 & 10000 \text{ bar} \cdot \frac{100 \text{ kPa}}{\text{bar}} \cdot \frac{1000 \text{ Pa}}{\text{kPa}} \\ \text{kPa} &= 1.0 \times 10^6 \end{aligned}$$

2. The following is a listing of the average densities of the atmosphere, hydrosphere and lithosphere:
 0.001225 g/cm^3 $D_{\text{water}} = 1 \text{ g/cm}^3$ $D_{\text{rock}} = 2.7 \text{ g/cm}^3$

$D_{\text{air}} =$

Calculate the following density equivalents:

$$\begin{aligned} D_{\text{air}} &= 1.225 \text{ kg/m}^3 & 0.001225 \frac{\text{g}}{\text{cm}^3} \cdot \frac{\text{kg}}{1000 \text{ g}} \cdot \frac{100^3 \text{ cm}^3}{\text{m}^3} \\ D_{\text{water}} &= 1000 \text{ kg/m}^3 & 1 \cdot \frac{\text{kg}}{1000 \text{ g}} \cdot \frac{100^3 \text{ cm}^3}{\text{m}^3} \\ D_{\text{rock}} &= 2700 \text{ kg/m}^3 & 2.7 \cdot \frac{\text{kg}}{1000 \text{ g}} \cdot \frac{100^3 \text{ cm}^3}{\text{m}^3} \end{aligned}$$

Calculate the following weight density equivalents (aka specific weight):

$$\begin{aligned} D_{\text{air}} &= 12.005 \text{ N/m}^3 & 1.225 \frac{\text{kg}}{\text{m}^3} \cdot 9.8 \text{ m/s}^2 \\ D_{\text{water}} &= 9800 \text{ N/m}^3 & 1000 \frac{\text{kg}}{\text{m}^3} \cdot 9.8 \text{ m/s}^2 \\ D_{\text{rock}} &= 26460 \text{ N/m}^3 & 2700 \frac{\text{kg}}{\text{m}^3} \cdot 9.8 \text{ m/s}^2 \end{aligned}$$

3. Average ocean salinity is approximately a 3.5% solution of dissolved salts and ions (Cl, Na, Mg, Ca). Given that the density of water is 1 g/cm³, and that 1 cm³ = 1 ml in volume equivalents, determine the density of water in Kg/L.

$$D_{\text{water}} = \underline{1} \text{ kg/L} \quad 1 \text{ g/cm}^3 \cdot \frac{\text{kg}}{1000 \text{ g}} \cdot \frac{1 \text{ cm}^3}{\text{mL}} \cdot \frac{1000 \text{ mL}}{\text{L}}$$

- a. What is the percent concentration of a salt solution in which 1 kg of salt is dissolved in 1 L of water (%concentration = mass of solute / mass of solvent x 100%).

$$1 \text{ kg/L} \cdot 1 \text{ L} = 1 \text{ kg water} \quad \frac{1 \text{ kg salt}}{1 \text{ kg water}} \cdot 100 = \boxed{100\%}$$

- b. Determine the following concentrations of a saline solution in which 5 g of salt is dissolve in 1 liter of water:

$$\begin{aligned} \text{ppt} & \underline{5} & 1 \text{ L} \cdot 1 \text{ kg/L} &= 1 \text{ kg water} & \frac{0.005 \text{ kg}}{1 \text{ kg}} \cdot 100 &= 0.5\% \\ \text{ppm} & \underline{5000} & 5 \text{ g} \cdot \frac{\text{kg}}{1000 \text{ g}} &= 0.005 \text{ kg salt} & & \\ \text{ppb} & \underline{5 \times 10^6} & \frac{0.5 \text{ parts}}{100} \cdot \frac{1000}{1} & & \frac{0.5 \text{ parts}}{100} \cdot \frac{1 \times 10^6}{1} &= \frac{0.5 \text{ parts}}{100} \cdot \frac{1 \times 10^9}{1} \end{aligned}$$

4. A storage tank holds 500,000 gallons of water with an input of 50 cfs and output of 73 cfs. Determine the following:

- Inflow 22440 gpm
- Outflow 2.06×10^6 cms
- Change in storage flux per unit time 23 cfs
- How much water is gained or lost from the storage tank after 1.3 hours?

$$\begin{aligned} & \underline{805147} \text{ gallons} \\ & \underline{107640} \text{ cubic feet} \\ & \underline{3.050 \times 10^6} \text{ kg} \end{aligned}$$

$$50 \frac{\text{ft}^3}{\text{s}} \cdot \frac{7.48 \text{ gal}}{\text{ft}^3} \cdot \frac{60 \text{ s}}{\text{min}}$$

$$73 \frac{\text{ft}^3}{\text{s}} \cdot \frac{\text{m}^3}{35.31 \text{ ft}^3} \cdot \frac{100^3 \text{ cm}^3}{\text{m}^3}$$

$$73 - 50 = 23 \frac{\text{ft}^3}{\text{s}} \cdot \frac{3600 \text{ s}}{\text{hr}} \cdot 1.3 \text{ hr} = 107640 \text{ ft}^3 \cdot \frac{7.48 \text{ gal}}{\text{ft}^3} = 805147 \text{ gal}$$

$$1 \text{ kg/L} \cdot 805147 \text{ gal} \cdot \frac{\text{L}}{0.264 \text{ gal}} = 3.050 \times 10^6 \text{ kg}$$